“Chaos, Complexity, and Entropy”

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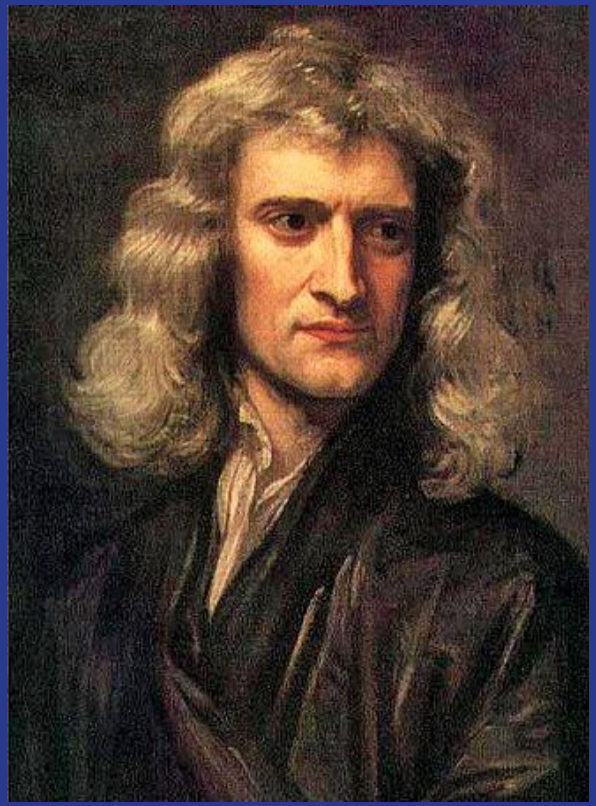
Sitpor.org/Abbas

Chaos

Chaos is the anti-calculus revolution.



Portrait of Newton in 1689 by Godfrey Kneller - *wikipedia*

Calculus is all about:

$y = f(x)$

For smooth and simple f.

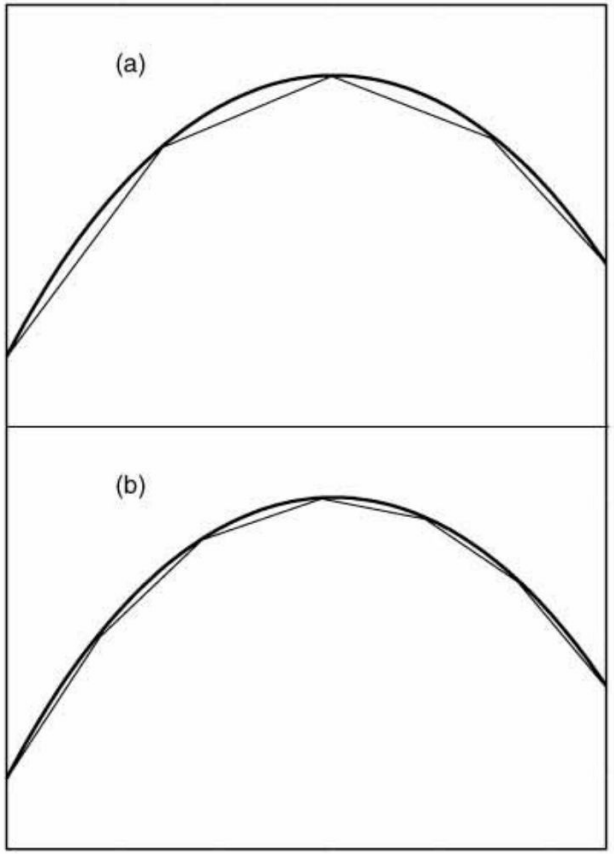
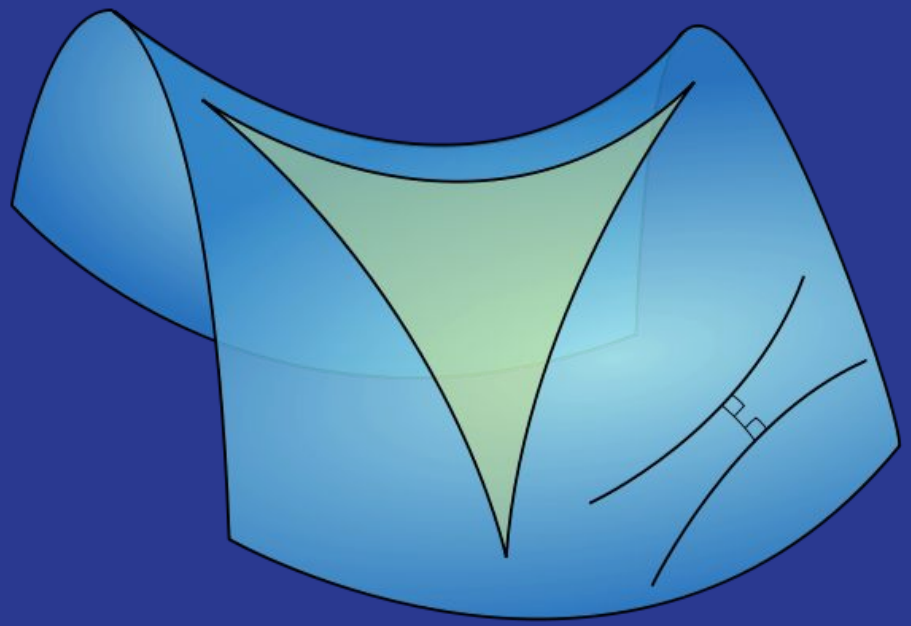
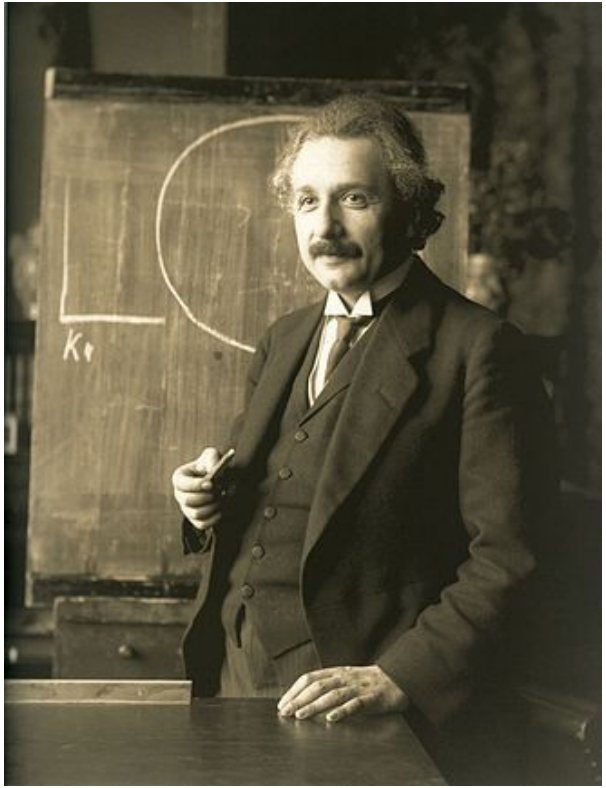


Figure 1: *The first and last calculus lesson.*



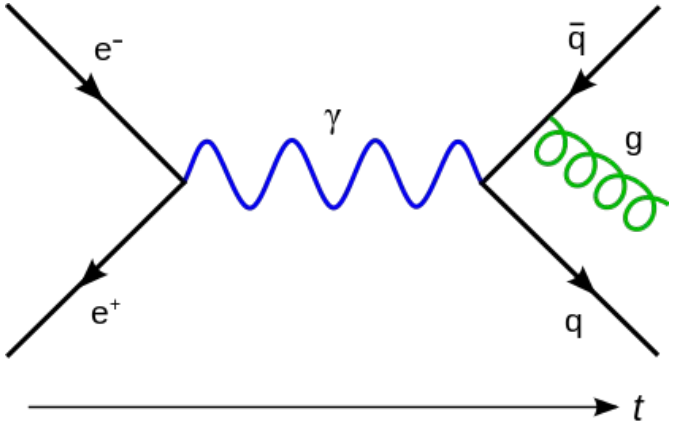
A triangle immersed in a saddle-shape plane (a hyperbolic paraboloid), as well as two diverging ultraparallel lines. *Wikipedia*

QM & QFT, both based on Calculus!



Albert Einstein in 1921 – *Wikipedia*

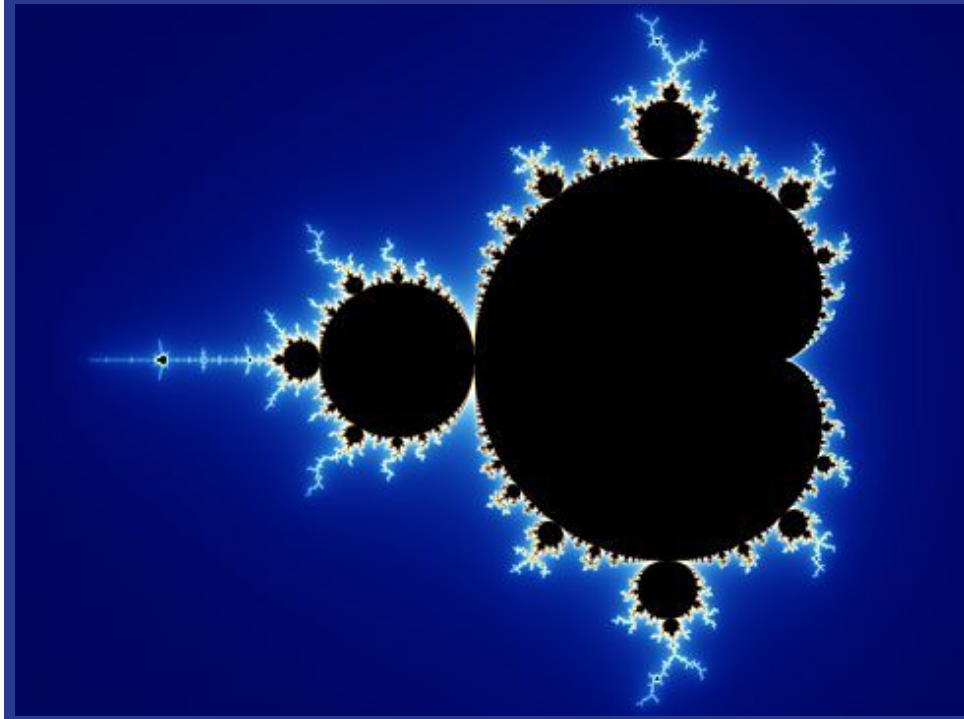
$$\langle \psi(t) | \frac{\partial}{\partial t} \psi(t) \rangle = \langle \psi(t) | \hat{H} \psi(t) \rangle$$



- ***Fractals are chaos in space!***

Sierpinski triangle – *Wikipedia*

- ***Fractals are chaos in space!***
- ***But not always self-similar***



Initial image of a Mandelbrot set zoom sequence with a continuously colored environment - *Wikipeda*

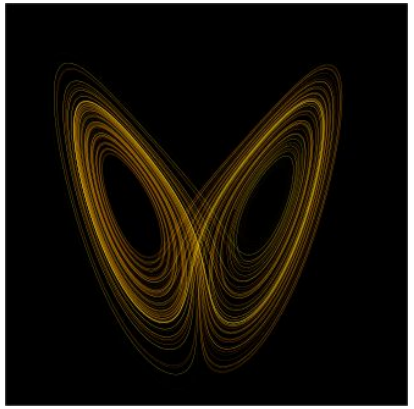
- ***The signature of time-chaos is something called "sensitivity to initial conditions".***

Edward lorenz – *Wikipedia*

Sensitivity to initial conditions is the death of reductionism!

- ***Every chaotic dynamical system is a fractal-manufacturing machine.***

- ***Conversely, every fractal can be seen as the possible result of the prolonged action of time-chaos.***

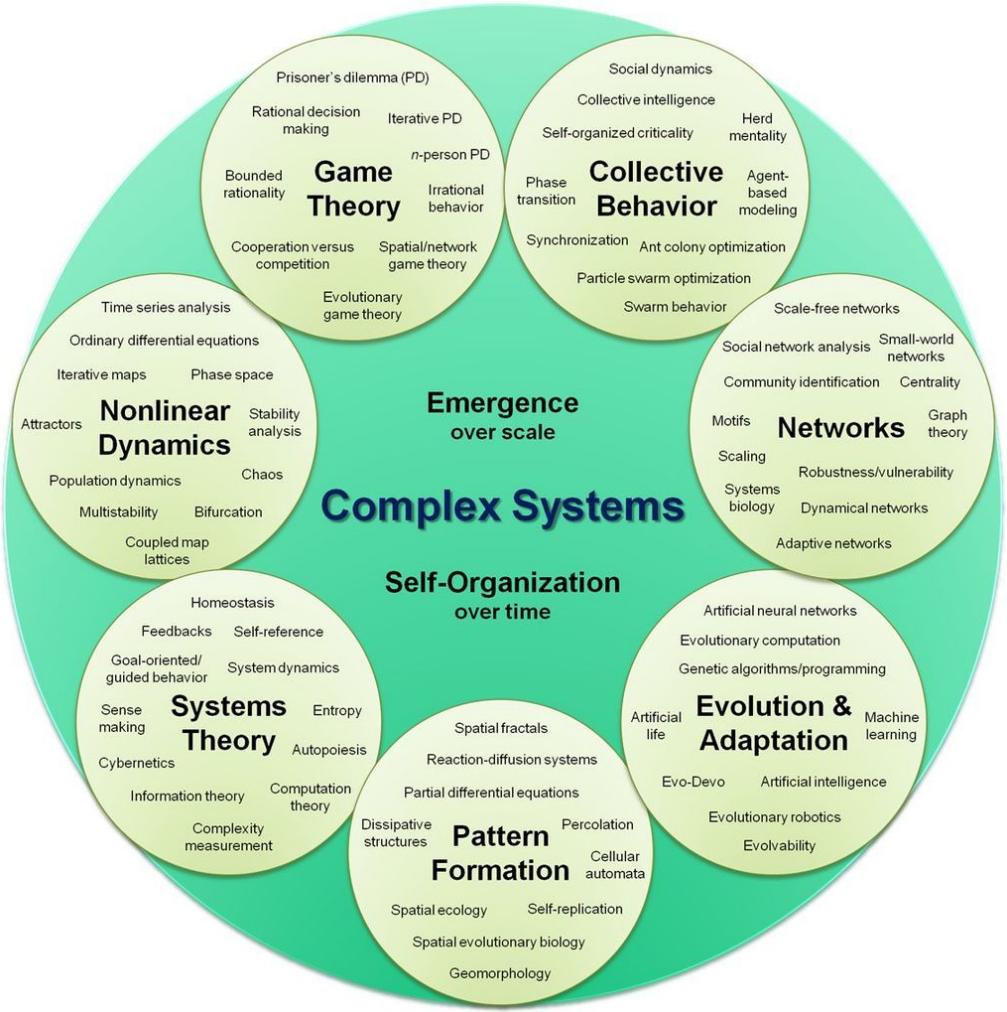


Lorenz System- *Wikipedia*

$$\frac{\mathrm{d}x}{\mathrm{d}t} = \sigma(y - x),$$
$$\frac{\mathrm{d}y}{\mathrm{d}t} = x(\rho - z) - y,$$
$$\frac{\mathrm{d}z}{\mathrm{d}t} = xy - \beta z.$$

Complexity!

Oh, yeah!, see: sitpor.org


Complex Systems
Emergence
over scale
Self-Organization
over time
Game Theory
Prisoner's dilemma (PD)
Rational decision making
Iterative PD
n-person PD
Bounded rationality
Irrational behavior
Cooperation versus competition
Spatial/network game theory
Evolutionary game theory
Collective Behavior
Social dynamics
Collective intelligence
Herd mentality
Self-organized criticality
Phase transition
Agent-based modeling
Synchronization
Ant colony optimization
Particle swarm optimization
Swarm behavior
Nonlinear Dynamics
Time series analysis
Ordinary differential equations
Iterative maps
Phase space
Attractors
Stability analysis
Population dynamics
Chaos
Multistability
Bifurcation
Coupled map lattices
Networks
Scale-free networks
Social network analysis
Small-world networks
Community identification
Centrality
Motifs
Graph theory
Scaling
Robustness/vulnerability
Systems biology
Dynamical networks
Adaptive networks
Systems Theory
Homeostasis
Feedbacks
Self-reference
Goal-oriented/ guided behavior
System dynamics
Sense making
Entropy
Autopoiesis
Cybernetics
Information theory
Computation theory
Complexity measurement
Evolution & Adaptation
Artificial neural networks
Evolutionary computation
Genetic algorithms/programming
Artificial life
Machine learning
Evo-Devo
Artificial intelligence
Evolutionary robotics
Evolvability
Pattern Formation
Spatial fractals
Reaction-diffusion systems
Partial differential equations
Dissipative structures
Percolation
Cellular automata
Spatial ecology
Self-replication
Spatial evolutionary biology
Geomorphology

Entropy

*Did anyone say Hail **Boltzmann?!***

$$S = k. \log W$$

Boltzmann's grave in the Zentralfriedhof, Vienna, with bust and entropy formula. – *Wikipedia*

“The paradox of the Arrow of Time”

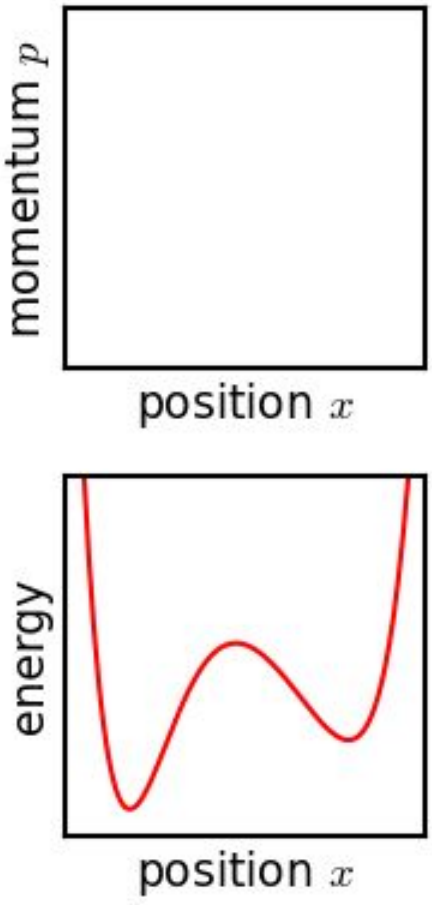
Unsolved problem in physics:

? *What links the quantum arrow of time to the thermodynamic arrow?*

(more unsolved problems in physics)

Liouville's Theorem

Evolution of an ensemble of classical systems in phase space (top). Each system consists of one massive particle in a one-dimensional potential well (red curve, lower figure). Whereas the motion of an individual member of the ensemble is given by Hamilton's equations, ***Liouville's equations describe the flow of the whole distribution.*** *The motion is analogous to a dye in an incompressible fluid.*



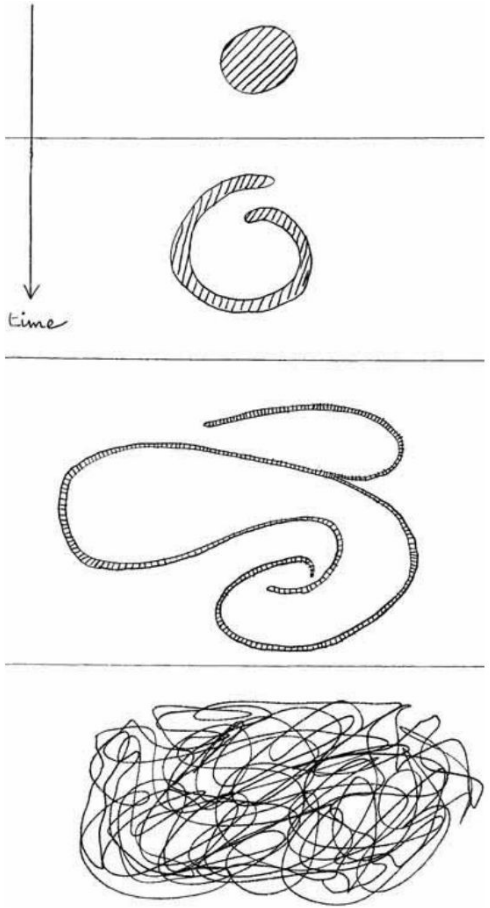


Figure 4: *The time evolution of a simple region of phase space turns it into a fractal.*

Where Does Complexity Come From?

http://www.aparat.com/v/84ncH

Resources

Chaos, Complexity, and Entropy

A physics talk for non-physicists

Michel Baranger

Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics
Massachusetts Institute of Technology, Cambridge, MA 02139, USA
and
New England Complex Systems Institute, Cambridge, MA 02138, USA
MIT-CTP-3112

Fractals:

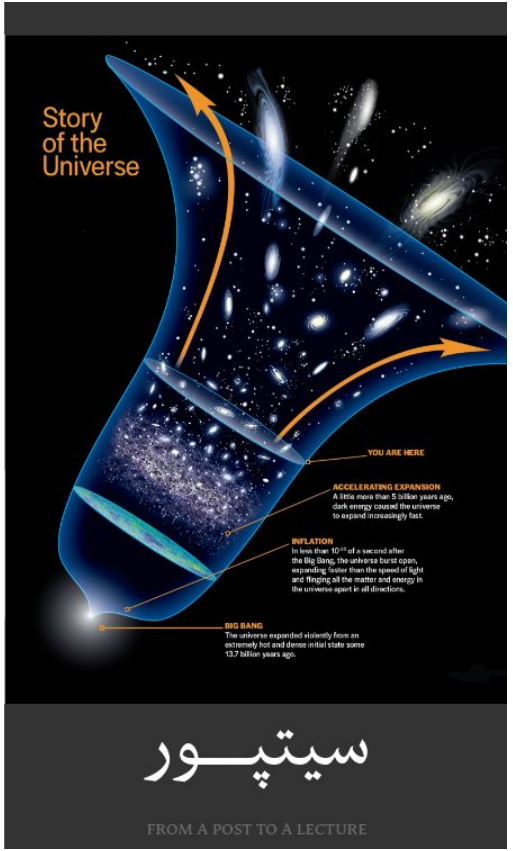
نوشته‌های دنباله‌دار

۱- فرکتال‌ها (برخال‌ها – fractals):

«هندسه‌ی فرکتالی، فقط بخشی از ریاضیات نیست، بلکه موضوعی است که به هرکس کمک می‌کند تا این دنیا را متفاوت ببیند.» بنوا مندلبرو – پدر هندسه‌ی فرکتالی

- قسمت اول) مقدمه و معرفی
- قسمت دوم) ویژگی‌ها و تعاریف
- قسمت سوم) خم‌های فضاپرکن و فرکتال‌های تصادفی
- قسمت چهارم) مجموعه ژولیا
- قسمت پنجم) مجموعه مندلبرو

۲- آموزش آنلاین، معرفی کتاب و دوره:



TEXTBOOKS

For the technically inclined, here are a few good books.

Steven H. Strogatz, *Nonlinear Dynamics and Chaos* (Addison-Wesley, Reading, 1994).
Undergraduate level. Mostly about dissipative chaos. Quite entertaining.

L.E. Reichl, *The Transition to Chaos*, (Springer, New York, 1992).
Graduate level. Mostly about conservative chaos. Very complete. Includes quantum chaos.

Yaneer Bar-Yam, *Dynamics of Complex Systems* (Addison-Wesley, Reading, 1997).
Invaluable. Very wide range of topics.

Roger Balian, *From Microphysics to Macrophysics*, 2 volumes (Springer, Berlin, 1991–2).
A thorough introduction to statistical mechanics.

Thanks!

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